

## Important Questions of Chapter 8

### Subject-Mathematics

#### Class-X

1. If  $\sec \theta = \frac{25}{7}$ , Find the value of  $\tan \theta$  and  $\operatorname{cosec} \theta$ .
2. In  $\triangle ABC$ , right angle at B, if  $AB=12$  cm and  $BC=5$ cm, find (i)  $\sin A$  and  $\tan A$ , (ii)  $\sin C$  and  $\cot C$ .
3. If  $3 \tan \theta = 4$ , find the value of  $\frac{5 \sin \theta - 3 \cos \theta}{5 \sin \theta + 2 \cos \theta}$ .
4. In a triangle ABC, right angled at B, the ratio of AB to AC is  $1 : \sqrt{2}$ . Find the value of  $\frac{2 \tan A}{1 + \tan^2 A}$ .
5. In the figure below,  $\triangle ABC$  is right angled at b,  $BC=7$  cm and  $AC-AB=1$  cm. Find the value of  $\cos A + \sin A$ .
6. If  $\sin \theta = x$  and  $\sec \theta = y$ , then find the value of  $\cot \theta$ .
7.  $\triangle RPO$  is a right angled at Q. If  $PQ=5$ cm and  $RQ=10$ cm, find: (i)  $\sin P$  (ii)  $\cos^2 R$  and  $\tan R$  (iii)  $\sin P \times \cos P$  (iv)  $\sin^2 P - \cos^2 P$ .
8. If  $\sin \theta = \cos \theta$ , find the value of  $\theta$ .
9. If  $\tan \theta = \frac{1}{\sqrt{3}}$ , then evaluate  $\left[ \frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta} \right]$
10. If  $\sin(A-B) = \frac{1}{2}$ ,  $\cos(A+B) = \frac{1}{2}$ , find A and B.
11. If  $\sqrt{3} \sin \theta - \cos \theta = 0$  and  $0^\circ < \theta < 90^\circ$ , find the value of  $\theta$ .
12. If  $A=60^\circ$  and  $B=30^\circ$ , verify that  $\sin(A-B) = \sin A \cos B - \cos A \sin B$ .
13. Evaluate :  $4 \cot^2 45^\circ - \sec^2 60^\circ + \cos^2 90^\circ$ .
14. Evaluate:  $\frac{2 \cos^2 90^\circ + 4 \cos^2 45^\circ + \tan^2 60^\circ + 3 \operatorname{cosec}^2 60^\circ + 1}{3 \sec 60^\circ - \frac{7}{2} \cos^2 45^\circ + 2 \operatorname{cosec} 30^\circ - 1}$
15. Evaluate :  $\frac{4}{\cot^2 30^\circ} + \frac{1}{\sin^2 60^\circ} - \cos^2 45^\circ$
16. If  $\tan \frac{5\theta}{2} = \sqrt{3}$  and  $\theta$  is acute, then find the value of  $2\theta$ .
17. If  $\sqrt{3} \sin \theta = \cos \theta$ , find the value of  $\frac{3 \cos^2 \theta + 2 \cos^2 \theta}{3 \cos^2 \theta + 2}$
18. Find the value of  $\theta$  ( $0^\circ < \theta < 90^\circ$ ) if  $2 \cos^2 \theta = \frac{1}{2}$ .
19. If  $\sin A = \cos A$ , find the value of  $2 \tan^2 A + \sin^2 - 1$ .
20. In an acute angled triangle ABC, if  $\sin(A+B-C) = \frac{1}{2}$  and  $\cos(B+C-A) = \frac{1}{\sqrt{2}}$ , find  $\angle A$ ,  $\angle B$  and  $\angle C$ .
21. Give that  $\cos(A-B) = \cos A \cdot \cos B + \sin A \cdot \sin B$ , find the value of  $\cos 15^\circ$  in two ways.  
(i) Taking  $A = 60^\circ$ ,  $B = 45^\circ$  and  
(ii) Taking  $A = 45^\circ$  and  $B = 30^\circ$
22. If  $\sec A = \frac{15}{7}$  and  $A+B=90^\circ$ , find the value of  $\operatorname{cosec} B$ .
23. Prove without using trigonometric tables:  $\sin^2 5^\circ + \sin^2 10^\circ + \dots + \sin^2 85^\circ + \sin^2 90^\circ = 9 \frac{1}{2}$   
[HOTS]
24. Prove without using trigonometric tables:  $\frac{\cos(90^\circ - A) \cdot \sin(90^\circ - A)}{\tan(90^\circ - A)} = \sin^2 A$
25. Prove without using trigonometric tables:  $\tan 10^\circ \cdot \tan 75^\circ \cdot \tan 15^\circ \cdot \tan 80^\circ = 1$
26. Evaluate :  $\frac{\sec^2(90^\circ - \theta) - \cot^2 \theta}{2(\sin^2 25^\circ + \sin^2 65^\circ)} + \frac{2 \sin^2 30^\circ \tan^2 32^\circ \cdot \tan^2 58^\circ}{3(\sec^2 33^\circ - \cot^2 57^\circ)}$
27. If  $A+B=90^\circ$ , Prove that  $\sqrt{\frac{\tan A \tan B + \tan A \cot B}{\sin A \sec B} - \frac{\sin^2 B}{\cos^2 A}} = \tan A$
28. Find  $\tan(65^\circ - \theta) - \cot(25^\circ + \theta)$
29. Find the value of  $\sin 38^\circ - \cos 52^\circ$
30. Evaluate:  $\sin \theta \cdot \sec(90^\circ - \theta)$

ASSIGNMENT ,CLASS X

MATHEMATICS

CHAPTER-9 APPLICATION OF TRIGONOMETRY

- Q:1 If the height of the shadow of a man are the same , then find the angle of elevation of the sun.  
(45°)
- Q:2 A pole 10m high casts a shadow 10m long on the ground. What is the elevation of the sun?  
(45°)
- Q:3 A ladder, leaning against a wall , makes an angle of 60° with the horizontal . If the foot of the ladder is 2.5 m away from the wall , find the length of the ladder. ( 5 m)
- Q:4 A ladder 15 m long just reaches the top of a vertical wall. If the ladder makes an angle of 60° with the wall, Find the height of the wall. (7.5 m)
- Q:5 What are the angles of depression of the object at E from the observation point A if AD = ED ? (45°)
- Q:6 If the length of the shadow of a tower is  $\sqrt{3}$  times its height, then find the angle of the elevation of the sun. (30°)
- Q:7 Find the length of the shadow on the ground of a pole of height 6m when the angle of elevation  $\theta$  of the sun is such that  $\tan \theta = \frac{3}{4}$  ( 8 m)
- Q:8 The angle of depression of car parked on the road from the top of a 150 m high tower 30°. Find the distance of the car from the tower. (150√3)
- Q:9 An observer 1.5 m tall is 20.5 m away from a tower 22m high. Determine the angle of elevation of the top of the tower from the eye of the observer. (45°)
- Q:10 The angle of elevation of an aeroplane from a point on the ground is 60°. After a flight of 15 seconds , the angle of elevation changes to 30°. If the aeroplane is flying at a constant height of 1500 √3 m , find the speed of the plane in km/hr. (720km/hr)
- Q:11 The angle of elevation of the top Q of a vertical tower PQ from a point X on the ground is 60°. From a point Y , 40 m vertically above X, the angle of elevation of the top Q of tower is 45°. Find the height of the tower PQ and the distance PX. (94.46, 54.6)
- Q:12 A boy Harpreet Singh standing on the top of a hotel, which is on the sea shore. Finds that a boat coming towards him takes 10 minutes for the angle of depression to change from 30° to 60°. How soon will the boat reach the sea shore ? (15 minutes)
- Q:13 A boy whose eye-level is 1.3 m from the ground , spots a balloon moving with the wind in a horizontal line at some height from the ground. The angle of elevation of the balloon from the eyes of the boy at an instant is 60° . After 2 seconds , the angle of elevation reduces to 30° . If the speed of the wind is 29√3 m/s , then find the height of the balloon from the ground.(88.3m)